

UNIVERSITY OF AUCKLAND

Advanced Computer Graphics

NPR - Shading of 3D models in cartoon-like style

NON-PHOTOREALSTIC-GRAPHICS

A tutorial on how to create cartoon shaded figures from 3D models

© Christian Graf
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e-mail: chrille.graf@gmx.de
homepage: <http://www.fam-graf.info>

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Introduction

Background information on NPR, shading and comics, and aims of this tutorial.

Non-photorealistic rendering tries to simulate the styles artists use, which includes i.e. for pen-and-ink or pencil illustrations, water colour drawings and engravings. Users and viewers can benefit from this artificial reproduction. It was shown that making images look less photorealistic enable audiences to feel more immersed and that meaning is more easily conveyed. By simplification and leaving out mess, one can amplify the effect of information relevant to the presentation (“amplification through simplification” [McCl93]). Additionally a wider audience will identify with those characters drawn in a simple style [MöHE02].

Comic-Rendering (a.k.a. toon-rendering, a.k.a. cartoon-rendering, a.k.a. cel-rendering) is one of the most vital areas of NPR with practical application in games such as *Jet Grind Ratio* and *Cel Damage* and image processing programs such as *Live Styles* from Viewpoint. It is about the possibilities of how to display a given object in the style a comic drawer would normally produce. In comics, objects are drawn with solid lines (silhouettes) separating areas of different solid colours [MöHE02]. There are no soft transitions from one coloured area to the next, but instead sharp edges. This effect is called toon shading.

This work on NPR is my contribution to the Research Frontiers part of the Advanced Computer Graphics Class at the Auckland University of 2002. My workgroup focused on the [Kaln02] paper and its details. Comic-rendering is one

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fundamental technique mentioned in that text and WYSIWYG is strongly related to real-time rendering. Thus I have chosen the topic for my tutorial. WYSIWYG is the reason for the implementation in OpenGL and not in an off-line ray tracing method, as one could choose as well for toon shading. For silhouette rendering there should be an in-depth tutorial available from Qinglei Meng (qmen002@ec.auckland.ac.nz). Another group member, Yuman Huang (yhua047@ec.auckland.ac.nz), has focused on stroke synthesis. This topic is challenging too, as there are different types of strokes in NPR, which have to be synthesized efficiently and are asked to be convenient to use. For details in both fields you are warmly welcomed to have a look into the others' tutorials.

Objectives

The tutorial: extent, content, prerequisites, and expected results.

In this tutorial the question how to do toon shading is covered. We focus on real-time rendering, not ‘offline’ ray tracing. From the current point of research we will see how to create that specific effect of toon shading and what enhancements could be applied. We will talk in detail about which methods and data structures are beneficial to achieve a good toon shaded impression whilst not decreasing the performance of the system.

The student is asked to undertake his own experiments with the programs he has compiled from this tutorial. Working with NPR is always a question of using the correct parameters, which normally cannot be found algorithmically. Thus the student should ‘play around’ with his code and compose new effects by varying parameters.

The guiding question should be how convenient the output under the chosen parameters represents the vital features of the object. Those must be evaluated ‘by hand’ through looking at the result, as it is the user who should interpret it. We should always keep in mind that real-time operation is expected, which means that all computations are time critical. Programming background in OpenGL and C is helpful to accomplish the tutorial but not compulsory as well as initial knowledge of linear algebra in vector space.

Taking this tutorial shall show the reader how to create a simplified scene by the use of toon shading. He is expected to notice the change in the output, which results in the amplification of the target features.

Methods

Approaches to the shading problem, data structures, exploiting graphics hardware

Cartoon figures are in contrast to other characters from our every-day experience intentionally two-dimensional. “Rather than shading the character to give it a three- dimensional appearance, the cartoonist typically uses solid colours that do not vary across the material they represent.” [Lake97] Not using Gouraud’s or Phong’s model which use smoothly interpolating shading, colour or tone is converted to discrete levels. This section shows the basic mechanism behind toon shading and will probably give the reader an idea how to implement the necessary data structures and algorithms, which will be used in the next section.

For shading in comic representations two common methods are used: the polygonal areas are filled with solid (unlit) colour, thus the shading information is lost. Or, in the two-level approach: one colour represents the lit, the other the shadowed areas. The second colour is most often a darker version of the one for the main material. According to [Lake97] “this helps add lighting cue, cues to the shape and context of the character in a scene, and even dramatic cues. The boundary between shadowed and illuminated colours is a hard edge that follows the contours of the object or character.” That’s the reason why some authors call this technique “hard shading”.

The technique used for our toon shader should find a transition boundary between the lit and the unlit area and then fill each side with a solid colour. We adopt the formula for diffuse lighting, which holds for both, the smooth shading and the comic shading shown in Equation 1.

$$C_i = a_g \times a_m + a_l \times a_m + (\text{Max}\{L \bullet n, 0\}) \times d_l \times d_m$$

Equation 1

C_i is the colour at vertex i . The variables' names denote (a)mbient and (d)iffuse light whereas the subscripts denote the scope of the variables: (g)lobal, (l)ight and (m)aterial. L is the unit-vector from the light source to the vertex, and n is the unit normal to the surface at i . The extra factor $\text{Max}\{L \bullet n\}$ in the second cross-product makes the diffuse part of the term in-significant if the light ray hits the surface in an angle greater than 90° . Then the dot-product becomes negative and the whole term is 0. This is the case when light arrives from 'behind' the surface, which equals to shadow. That's exactly what Equation 1 simulates: no diffuse light is added to the ambient light. The experienced reader with background in computer graphics fundamentals may skip the next paragraph.

L is calculated through the normalized difference of the vector l from the origin to the light position with the vector p to the object point's position in world coordinates as shown in Equation 2.

$$L = \frac{p-l}{|p-l|} \quad p = \begin{bmatrix} p_x \\ p_y \\ p_z \end{bmatrix} \quad l = \begin{bmatrix} l_x \\ l_y \\ l_z \end{bmatrix}$$

Equation 2

Using the inner product of vector v , which calculates as Equation 3 shows, does the normalization of this vector.

$$|v| = \frac{v}{\sqrt{v_x^2 + v_y^2 + v_z^2}} \quad v = \begin{bmatrix} v_x \\ v_y \\ v_z \end{bmatrix}$$

Equation 3

An obvious approach to achieve cartoon style shading would be per-pixel procedural shading. But this is not beneficial, as the today's graphics hardware does not provide any support for such an operation. Another option would be a hardware driven tresholded variation of Gouraud shading. Unfortunately this is not

supported either. Thus we have to make up our minds for a more complex but evenly fast solution for the shading problem. Instead of calculating the colours per vertex, we create a 1D texture map of a minimal number of colours. Without any advanced features like highlights (see later part of this tutorial) this minimal number should be two: one for the shadowed colour, one for the illuminated colour, as shown in Figure 1. Note that the transition point between the two colours can be arbitrarily set, in this case at a value of 0.5, but this influences the appearance of the output to a great extent: the blacker the texture the darker will be the output image.



Figure 1

The brighter colour of the texture map is calculated as if it is directly lit. This means there would be an angle of 0 degrees between L and n . As the dot product is equal to the cosine of the angle between the two vectors, the term $L \bullet n$ in Equation 1 results in the value of 1. The modified equation for vertices with lit colour is shown in Equation 4.

$$C_i = a_g \times a_m + a_l \times a_m + d_l \times d_m$$

Equation 4

Accordingly the shadowed colour for texture map is calculated. If no direct light contributes to the shading, only the ambient part of lighting provides irradiance intensity. $L \bullet n$ is set to 0 in Equation 1, resulting in Equation 5, to simulate this.

$$C_s = a_g \times a_m + a_l \times a_m$$

Equation 5

As result we get a 1D texture as shown in Figure 1. It's computed once per material and stored before the rendering of the object starts. While rendering each frame we compute $Max(L \bullet n)$ at each vertex and use these per-vertex values as texture coordinates in our pre-computed texture map. The current vertex is then assigned with the colour value found in the texture map. After each image point was coloured accordingly, the whole image has been rendered.

T O O N - S H A D I N G

We have now seen how the methods which will lead us to our toon shaded object. The next section will show us how the implementation looks like. After that a few interesting problems and enhancement are mentioned before we come to the end and results of this tutorial.

Implementation

The methods we have got to know in the previous section should lead us to the realization of toon shading. In this section we will see, what steps we have to take to achieve a nice cartoon shaded object. We will first approach our aim more generally in pseudo code and then switch to OpenGL and its solutions.

ALGORITHM *Cartoon Shade*

Preprocess:

1. Calculate the illuminated diffuse color for each material:

$$C_i = a_g \times a_m + a_l \times a_m + d_l \times d_m$$

2. Calculate the shadowed diffuse color:

$$C_s = a_g \times a_m + a_l \times a_m$$

3. For each material, create and store a one-dimensional texture map with two texels using the texture functionality provided by a standard 3D graphics API. Color the texel at the u=1 end of the texture with C_i and the texel at the u=0 end of the texture with C_s .

Runtime:

1. Calculate the one-dimensional texture coordinate at each vertex of the model using $\text{Max}\{\mathbf{L} \cdot \mathbf{n}, 0\}$, where \mathbf{L} is the normalized vector from the vertex to the light source location, \mathbf{n} is the unit normal to the surface at the vertex, and $\mathbf{n} \cdot \mathbf{L}$ is their vector inner (dot) product.
2. Render the model using a standard graphics API with lighting disabled and one-dimensional texture maps enabled.

Toon shading pseudo code according to [Lake97]

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From the pseudo code we can learn that a major part of toon shading takes place before the actual rendering is done. The reason for that is the different way toon shading has to find the colour for the vertex, as explained in the former section. In our example implementation step one and two of the preprocess are omitted for the sake of simplicity. Otherwise all the properties of the material have to be known. But in most circumstances this is not the case.

We starts with the 1D texture map. It is 'hard coded' (part of the code, not variable) as an array `texture` and for every object and material the same (in our scenes there is only one object at time). In contrast to the pseudo code, the 1D structure is expanded to be able to hold all three base colours. In this way it is possible to store colour and tone in one step. Otherwise we would have to compute the shading as fraction of black (or white) and then multiply it with all three basic colours to get the result. That's far too slow and unnecessary as the resulting colours are only the two distinct toon shades.

To use such a texture one has to create and bind it to a certain variable of type `GLuint`, a special type of OpenGL. This is done in the `init()` method.

```
glGenTextures(1, &textureID);  
glBindTexture(GL_TEXTURE_1D, textureID);
```

After this step we must define how the 'behaviour' of our texture should be if mapped to an area where a texel does not exactly correspond to a pixel or a whole texture is too small or too big. Such a command looks similar to the following.

```
glTexParameteri(GL_TEXTURE_1D, GL_TEXTURE_MAG_FILTER,  
GL_NEAREST);
```

Basically this means that a texture magnification function is used when the pixel being textured maps to an area less than or equal to one texture element and that the value of the texture element that is nearest (in Manhattan distance) to the center of the pixel being textured will be returned.

Finally we really specify our texture image using the type of texture (`GL_TEXTURE_1D`), the dimensions, the type of colour in it (`GL_RGB`), the type of texture (`GL_UNSIGNED_BYTE`) and the structure where the data for the texture can

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be found (`texture`). The last parameter is our constructed pre-computed array of data type `GLubyte`.

```
glTexImage1D(GL_TEXTURE_1D, 0, GL_RGB, 4, 0, GL_RGB,  
GL_UNSIGNED_BYTE, texture);
```

Now we have finished the pre-computation phase and can go into the rendering. An OpenGL program does loop all the time, which means, that code bound to so call-back function in that loop is executed over and over again. We don't have to worry about that. Each time when the program reaches the part where the drawing is done (`display()`), we have to get sure that our object is processed and shown on the screen.

The first step is to enable the texture functionality and to bind the texture again

```
glEnable(GL_TEXTURE_1D);  
glBindTexture(GL_TEXTURE_1D, textureID);
```

In this step additional options can be set as well. But they are not relevant here. The normal lighting is then 'switched off' which means that the current lighting parameters to compute the vertex color or index are not used anymore (because we want our own special light which results in toon shading).

```
glDisable(GL_LIGHTING);
```

After that our model can be drawn. We read our model from an `.OBJ` file, a format which can be written by Alias Wavefront, one of the big 3d modeler applications. The code for the parser `glm.c` was written by Nate Robins. With it we get all the points and their connections from a file. What we need for the calculation of shading are the normals. Luckily the parser generates the average normal for each vertex by itself, so we don't have to bother with the cross-product to get them by ourselves.

For each group of triangles in the model we sequentially take the three vertices of one triangle after the other. Then we get the normalized average normal for each vertex. With this data we can compute a texture co-ordinate into our pre-computed texture map.

```
glTexCoord1f(maxNdotL(n, light));
```

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n is the normal of the vertex and $light$ is the vector to the light. $maxNdotL$ is the accurate implementation of the function $\mathbf{Max}\{L \cdot n, 0\}$. The command as whole sets the current texture coordinate that is part of the data associated with the polygon vertex (our texture!) according to the result of the $maxNdotL(n, l)$ function.

```
maxNdotL(float n[3], float l[3]) = {  
    if (l[0]*n[0]+l[1]*n[1]+l[2]*n[2]) > 0.0)  
    then (l[0]*n[0]+l[1]*n[1]+l[2]*n[2])  
    else 0.0; }
```

Thus the colour of the vertex is found and the vertex' representation written to the screen. After all the faces with their vertices were processed the whole patch is done and the object has been rendered.

The last step is to disable texture mapping and switch on lighting again. This is necessary because other objects may need another environment and other lighting conditions. Without explicit deactivation they would be trapped in the current configuration.

Our methodological reflections in the beginning of this tutorial have guided us to this nice implementation of toon shading. For further details in OpenGL see [OpenGL]. Figure 2 shows a possible outcome of the algorithm. Here we have three colours in the shading, one depicts highlights. This seems more elaborated but it is easily to be done, as you can read in the next section.



Figure 2: Two results of the algorithm

Reflection

Problems, enhancements, variations & further research

Problems

NPR techniques typically seek to realize three effects: tone, texture and outline. A minor general limitation in comic rendering results from the fact that tone and texture can't be completely separated and independently used to impart knowledge or meaning. In comic renderings tone overrides texture as it's only a solid colour which fills a whole area and hides further detail. Furthermore outlines are drawn using different strokes. It might appear as if they have texture (one might think of broad pencil strokes) and convey tone (because the cover a reasonable part of the canvas). But one must ask oneself if this is not a direct conclusion from the basic approach NPR takes: amplification by simplification. Information is omitted so one can expect a certain amount of detail is left out which benefits to the impression of the image as comic rendering. Recognized as such the viewer will not expect high detail and will gain another view on the image on the world behind it. The open question is how many features have to be absent or how many could be still present till the viewer depicts the image as comic like.

The hugest obstacle with the implementation is to overcome the current OpenGL specification. Today's graphics cards support OpenGL instruction on a hardware basis. They do not include any native NPR algorithm, but new code must be implemented in the application by the developer. This has the main drawback that user code is never executed as fast as hardware implemented routines. Additionally the design of applications would be eased and software engineering matters such as interoperability would be more conveniently met if NPR

algorithms were included. “Our texture-mapped method is equivalent to per-pixel colour tresholding. Without texture mapping we would need either hardware-supported per-pixel procedural shading or a tresholded variation of hardware Gouraud shading to achieve the same fast results.” [Lake97] The algorithm calculates a dot product at each vertex for every frame. With the current processors available this is done fast enough to ensure interactive display rates on scenes with realistic geometric complexity. But the dot product is calculated twice: once in our application, a second time in the graphics hardware for lighting. With a pathway from the lighting to the texture subsystem and an automatic texture-coordinate generation mode this double work would be omitted. Have a closer look at [Mohr02] for opportunities how to overcome some of the other mentioned limitations of OpenGL. It’s proposed there to directly intercept the graphic’s pipeline stream which would make NPR styles possible and fast at the hardware level.

The colour quantisation or texture-mapping can lead to stair-case effects or to fuzzy-borders. Therefore one aim is to get smooth transition borders between bi-tonal coloured regions of the object. One solution is to refine the whole object and decrease the size of the faces. In fact that does not really solve but only shrinks the problem and reduces the performance noticeable. Texture mapping gives either to aliased results or has too fuzzy borders between the cartoon-colours.

Enhancements & Variations

The just mentioned problem can be handled by sub-division of a face, which has more than one colour at its vertices, according to [Claes]. If i.e. a face with three colours exists, it’s sub-divided in three triangles. The new vertices are found by linear interpolation of the colour values along the triangle edges. The new face is assigned with the colour of the closest vertex.

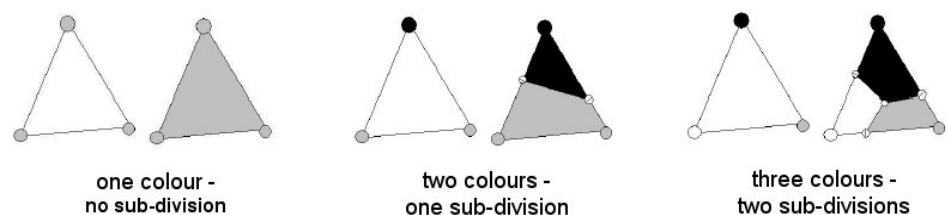


Figure 3: Different types of subdivisions.

The result of a successful sub-division process is shown in Figure 3 and applied in Figure 4 and 5.

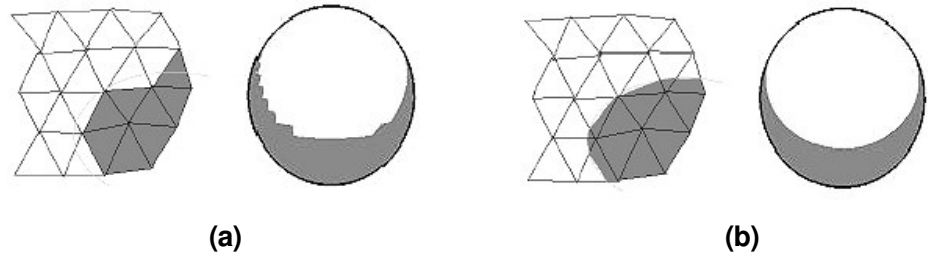


Figure 4: Principle of polygon subdivision. (a) without (b) without subdivision. Result on a sphere.



Figure 5: A deer rendered (a) without and (b) with subdivision.

A second method may help if transition borders of textures still look jagged if viewed closely. Depending on the geometry and the viewing condition texture

filtering can have benefits. It smooths the colour transition by a linear interpolation among a set of texels (texture elements) nearest to the pixel.

To enhance NPR drawings even more, we use the fact that silhouettes and creases with “higher levels of anti-aliasing produce better results. Insufficient anti-aliasing is particularly noticeable where ink lines are drawn: the lines chatter during animation.” [ClaeXX] An (still) example is shown in Figure 5.

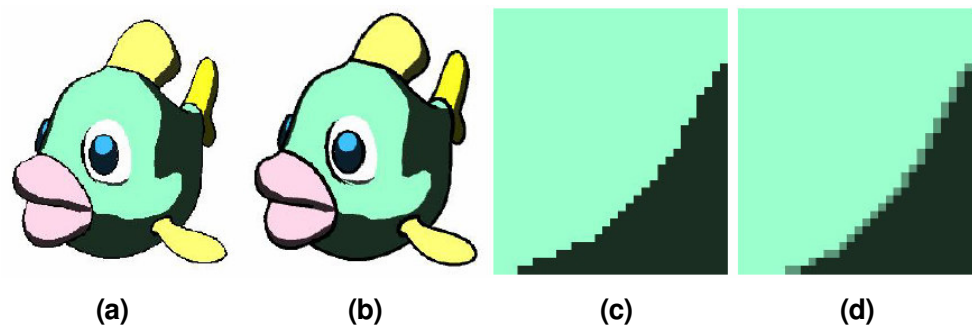


Figure 6: A rendering (a) without (b) with anti-aliasing turned on. (c,d) zoom-ins in (a,b)

Additional effects can be created by using other texture maps, i.e. with a higher resolution. In the case of a two-colour texture map, more texels can provide flexibility in the location of the shadow boundary. Let’s say that three out of four texels are assigned with the background colour and only one with the foreground colour (Figure 4).



Figure 7: texture map with four texels, giving the ‘dark comic’ style

Rendering an object with this map will give a result which appears to be more darkened because more pixels are set to the shadow colour than to the illuminated colour. Such setting can help to imitate a dark comic book feeling. Another rewarding option is to design the texture map with both ends in illumination colour and only the middle in shadow colour. This will lead to the effect which is normally achieved by double source lighting.

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The two-tone method for cartoon shading cannot display any highlights in the image, but it can be modified to do so. The 1D texture map is expanded to three colours by an additional one for the highlights. For convenient results we again use a higher resolution texture map. At the one end of the map a small portion of the texels is set to the highlight colour, at the other end a huge amount is assigned with the shadow colour and the rest in-between with the illuminated colour, as shown in Figure 5.

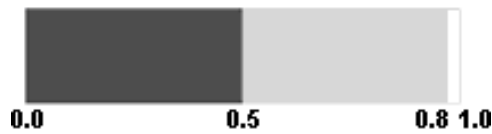


Figure 8: texture map with four texels, giving a highlight colour

The highlight colour can be chosen automatically by multiplying the standard object colour with a certain factor. As the highlights resulting from this technique are viewer independent, we call them “diffuse highlights”. To introduce viewer dependent specular highlights a second texture map has to be added. The appropriate texture coordinates for the new map come from a viewer dependant specular computation rather than from a diffuse one as above. The first and the second texture are blended together in a single rendering pass using multi-texturing, which is supported by today’s graphics hardware.



Figure 9: Olaf in 'dark comic' style with highlights shown

In contrast to other NPR techniques, which typically aim on the creation of tone, outline and texture, the basic comic rendering is only designed to achieve the first both effects. Texture is not introduced, which might have been deliberately avoided to contribute to the simple appearance of the characters and all the related advantages. But one could think of situations in which texture might aid to distinguish objects quickly, e.g. if the scene becomes too complex to be rendered with just two colours per object. One possible solution for this problem could be to use a 2D texture map which would provide a real texture, not only a colour. Another solution could be to use procedural textures and map them to the object's surface. Both solutions alter the shader which then still works real-time. Differently Halper et al. [Halp02] propose a way how to incorporate different NPR styles in one interface. Their approach is more general in terms of methods covered but is restricted to still images.

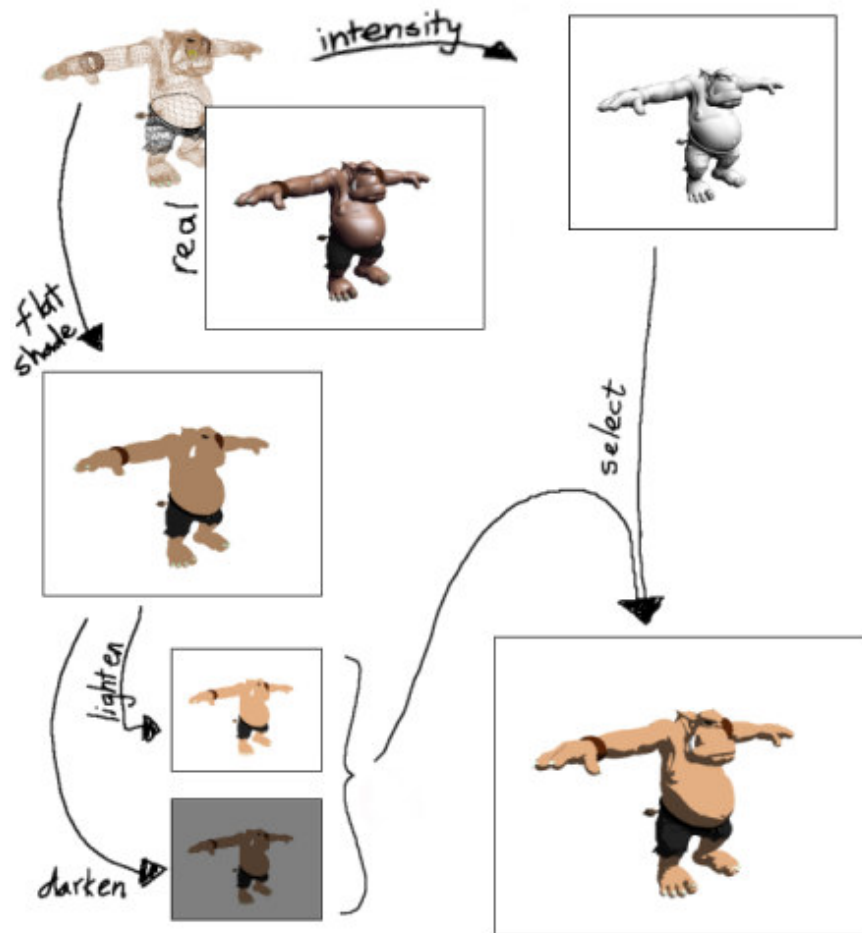


Figure 10: Step-by-Step shading of Olaf

With little modification the proposed solution for comic shading can be used to create pencil sketch drawings. The original algorithm is extended to handle two-dimensional textures. The inner product of light vector and surface normal is used to select a texture of appropriate density. Less light corresponds to more density and vice versa. Because this is a little out of scope I have mentioned it just shortly. For deeper insight have a look at [Lake97].

This section has made clear, that there are certain problems existing in the field of comic rendering and in particular for toon shading. Some of them are relevant for the implementation; some of them have a more general meaning in NPR. The reader should have noticed that there is a wide variety of enhancements and add-ons to toon shading and comic rendering which we were not able to cover here in detail. For further information have a look in the sources mentioned at the end of this tutorial or in the bibliography.

Results & Conclusion

In this tutorial we gave an introduction to non-photorealistic-rendering, what it does and how it works. We picked one distinguished style, comic rendering, and had a closer look at the method and implementation behind one of its parts: toon shading. As we could see, toon shading only makes no comic renderer. It's complemented by silhouettes and motion line rendering¹. The last section explained the current and general problems, but showed what enhancement could be applied to toon shading and comic rendering, both in methodical and computational terms.

For me it was great joy to see what can be achieved by simplifying images and how it is done. As one technique among other, toon-shading is in principle not that difficult and should be easily understood. This property makes toon-shading a good entry point into the world of NPR. Consequently I wrote the tutorial. It probably encourages the reader to undergo further training or research in the area. I believe that artistic rendering, as NPR is called sometimes, can provide an interesting, helpful and fun way to convey complex correlations to the limited human perception. It facilitates and supports understanding! This is fascinating. It seems simple in the beginning but when you go deeper you will find a lot of unsolved questions. These problems give you an idea about the potentials behind comic rendering and NPR. This potential is the area I want to explore in future

I hope that this tutorial has provided an attractive way to learn a bit about comic rendering. If you want to achieve more expertise in NPR and its related

¹ Speed line or motion line rendering is an invention and not mentioned very often as part of comic rendering. Nonetheless it's mentioned here, because the author believes in the upcoming importance of such details characteristic for comics as art form.

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techniques the most appropriate places to go are Craig Reynolds' or Amy Coochs pages with an overwhelming bunch of links to almost each and every adjacent

topic: <http://www.red3d.com/cwr/npr/>

<http://www.cs.utah.edu/npr/>

ACM SIGGRAPH, the biggest annual conference on computer graphics, is a good resource for further research too:

<http://portal.acm.org/>

Thank you for your attention!

Christian Graf

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